

No notes or calculators. You can leave an answer as a numerical expression without computing the final value. For example, this is a perfectly acceptable answer :

$((250 - 63)/(1 - e^{(-6*3.5)}) * \ln(27/168))$ . Show your work clearly !!

1. (1pt each) Circle the right answer(s) in each of the following questions. More than one answer could be correct - you have to mark ALL the correct answers to get full credit.

(i)  $A$ ,  $B$  and  $C$  are  $n \times n$  matrices. Then  $A(BC) = (AB)C$  is :

- (a) Always true      (b) Sometimes true, depends on  $A$ ,  $B$ ,  $C$       (c) Always false

(ii)  $A$  and  $B$  are  $n \times n$  matrices. Then  $AB = BA$  is :

- (a) Always true       (b) Sometimes true, depends on  $A$ ,  $B$       (c) Always false

(iii)  $A$  and  $B$  are  $m \times p$  matrices,  $C$  is a  $p \times n$ . Then  $(A + B)C = AC + BC$  is :

- (a) Always true      (b) Sometimes true, depends on  $A$ ,  $B$ ,  $C$       (c) Always false

(iv)  $A$  is an  $n \times p$  matrix and  $B$  is a  $q \times n$  matrix and  $p \neq q$ . Which of the following products can be defined :

- (a)  $AB$        (b)  $BA$

(v)  $A$  is an  $m \times p$  matrix and  $B$  is a  $p \times n$  matrix. Which of the following products can be defined :

- (a)  $AB$        (b)  $B'A'$  (recall that  $A'$  and  $B'$  denote the transpose matrices.)

2. (5 pts) Let  $A = \begin{bmatrix} -1 & 2 \\ 0 & -3 \end{bmatrix}$ ,  $B = \begin{bmatrix} 0 & 1 \\ 2 & 4 \end{bmatrix}$  and  $C = \begin{bmatrix} 1 & -2 \\ 1 & -1 \end{bmatrix}$ . Find a  $2 \times 2$  matrix  $D$  such that

$$3D - A = 2(D - C) + 3B.$$

$$3D - A = 2D - 2C + 3B$$

$$\rightarrow 3D - 2D = A - 2C + 3B$$

$$\rightarrow D = A - 2C + 3B$$

$$\rightarrow D = \begin{bmatrix} -1 & 2 \\ 0 & -3 \end{bmatrix} + 3 \begin{bmatrix} 0 & 1 \\ 2 & 4 \end{bmatrix} - 2 \begin{bmatrix} 1 & -2 \\ 1 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} -3 & 9 \\ 4 & 12 \end{bmatrix}$$